

Package: copulaSQM (via r-universe)

June 3, 2026

Type Package

Title Copula Based Stochastic Frontier Quantile Model

Version 0.1.0

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Description Estimation of a copula-based stochastic frontier quantile model using simulated likelihood methods.

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Encoding UTF-8

LazyData true

Imports ald, VineCopula, stats, graphics, MASS

RoxygenNote 7.3.3

Repository <https://woraphonyamaka.r-universe.dev>

Date/Publication 2026-02-26 18:00:47 UTC

RemoteUrl <https://github.com/woraphonyamaka/copulasqm>

RemoteRef HEAD

RemoteSha 0c53100a285db6cf6b1e1f03c7d11e7d3f624afb

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copSQM

*Copula-Based Stochastic Frontier Quantile Model***Description**

Estimates a copula-based stochastic frontier quantile model using simulated maximum likelihood. Dependence between the two-sided noise component and the one-sided inefficiency component is captured via a bivariate copula from the *VineCopula* package.

Usage

```
copSQM(Y, X, family, tau,
       RHO, LB, UB,
       RH02 = NULL, LB2 = NULL, UB2 = NULL,
       nSim = 50,
       seed = NULL,
       maxit = 10000)
```

Arguments

Y	A numeric vector of dependent variable observations.
X	A numeric matrix (or object coercible to a matrix) of explanatory variables. The intercept is added internally.
family	Integer specifying the bivariate copula family (see <i>VineCopula::BiCopPDF</i>). Examples include 1 = Gaussian, 2 = Student-t. Some copula families require a second parameter.
tau	Quantile level in (0, 1) for the asymmetric Laplace distribution (ALD).
RHO	Initial value of the first copula parameter (passed to <i>par</i> in <i>VineCopula</i>). Note that this parameter is not always a correlation; its interpretation depends on the chosen copula family.
LB	Lower bound for the first copula parameter RHO.
UB	Upper bound for the first copula parameter RHO.
RH02	Optional initial value of the second copula parameter (passed to <i>par2</i> in <i>VineCopula</i>). This is required for copula families that have two parameters (e.g. Student-t where RH02 represents degrees of freedom, and BB families where RH02 is a shape parameter). If NULL, a one-parameter copula is assumed.
LB2	Optional lower bound for the second copula parameter RH02. Must be supplied when RH02 is not NULL.
UB2	Optional upper bound for the second copula parameter RH02. Must be supplied when RH02 is not NULL.
nSim	Number of Monte Carlo draws used to approximate the likelihood integral for each observation. Larger values improve accuracy but increase computation time.
seed	Optional integer seed for reproducibility of the simulation draws used in the likelihood. If NULL, no seed is set.
maxit	Maximum number of iterations for the optimizer (<i>stats::optim</i> with "L-BFGS-B").

Details

The model follows the stochastic frontier decomposition

$$Y_i = x_i^\top \beta + v_i - u_i,$$

where v_i is a two-sided noise term and $u_i \geq 0$ is the inefficiency term. Both components are modeled using the asymmetric Laplace distribution (ALD) at quantile level τ , with u_i truncated to $(0, \infty)$.

Dependence between u_i and v_i is introduced through a bivariate copula density $c(\cdot, \cdot)$ from the VineCopula package. The log-likelihood is evaluated by simulating draws of u_i from the truncated ALD and approximating the likelihood integral by Monte Carlo averaging (nSim draws per observation).

When a two-parameter copula family is used, RHO2 must be provided along with bounds LB2 and UB2.

Value

A list with components:

result	A matrix of parameter estimates, standard errors, z-values, and p-values.
AIC	Akaike Information Criterion.
BIC	Bayesian Information Criterion.
Loglikelihood	Maximized log-likelihood value.
convergence	Convergence code returned by <code>stats::optim</code> . A value of 0 indicates successful convergence.

Author(s)

Woraphon Yamaka, Paravee Maneejuk and Nuttaphong Kaewtathip

References

Pipitpojanakarn, V., Maneejuk, P., Yamaka, W., & Sriboonchitta, S. (2016). Analysis of agricultural production in Asia and measurement of technical efficiency using copula-based stochastic frontier quantile model. In *International Symposium on Integrated Uncertainty in Knowledge Modelling and Decision Making* (pp. 701–714). Springer.

Pipitpojanakarn, V., Yamaka, W., Sriboonchitta, S., & Maneejuk, P. (2017). Frontier Quantile Model Using a Generalized Class of Skewed Distributions. *Advanced Science Letters*, 23(11), 10737–10742.

Examples

```
set.seed(123)

sim_data <- sfa_simu_quantile(
  n = 50,
  beta = c(1, 0.5, -0.3),
  sigV = 1,
```

```

    sigU = 1,
    tau = 0.5,
    family = 1,
    rho = 0.3,
    seed = 123
  )

model <- copSQM(
  Y = sim_data$Y,
  X = sim_data$X,
  family = 1,
  tau = 0.5,
  RHO = 0.3,
  LB = -0.99,
  UB = 0.99,
  nSim = 50,
  seed = 123
)
model

## Example with a two-parameter copula (e.g., Student-t: family = 2)
## Here RH02 typically represents degrees of freedom and must be bounded.
model_t <- copSQM(
  Y = sim_data$Y,
  X = sim_data$X,
  family = 2,
  tau = 0.5,
  RHO = 0.3,
  LB = -0.99,
  UB = 0.99,
  RH02 = 4,
  LB2 = 2.01,
  UB2 = 50,
  nSim = 50,
  seed = 123
)
model_t

```

sfa_simu_quantile

Simulation of Copula-Based Stochastic Frontier Quantile Model

Description

Generates simulated data from a copula-based stochastic frontier quantile model with asymmetric Laplace noise and a truncated asymmetric Laplace inefficiency term.

Usage

```
sfa_simu_quantile(n,
```

```

beta,
sigV,
sigU,
tau = 0.5,
family = 1,
rho = 0.5,
rho2 = NULL,
seed = NULL)

```

Arguments

n	Integer. Number of observations to simulate.
beta	Numeric vector of regression coefficients including an intercept. Its length must match the number of regressors plus one (intercept). This simulator generates two regressors, so <code>length(beta)</code> must be 3.
sigV	Positive numeric value. Scale parameter of the two-sided noise term V .
sigU	Positive numeric value. Scale parameter of the one-sided inefficiency term U .
tau	Quantile level in $(0, 1)$. Default is 0.5.
family	Integer specifying the bivariate copula family (see <code>VineCopula::BiCopSim</code>). Examples include 1 (Gaussian) and 2 (Student-t). Some families require a second parameter <code>rho2</code> .
rho	First copula parameter (passed to <code>par</code> in <code>VineCopula</code>). Interpretation depends on the copula family and is not always a correlation.
rho2	Optional second copula parameter (passed to <code>par2</code> in <code>VineCopula</code>). This must be provided for copula families that require a second parameter (e.g., degrees of freedom for the Student-t copula, or a shape parameter for BB copulas).
seed	Optional integer seed for reproducibility. If <code>NULL</code> , no seed is set.

Details

This function simulates data from the stochastic frontier model:

$$Y = X\beta + V - U,$$

where:

- V follows an asymmetric Laplace distribution (ALD) with location 0, scale `sigV`, and quantile level `tau`.
- U is a non-negative inefficiency term generated from an ALD distribution with location 0, scale `sigU`, and quantile level `tau`, truncated to $(0, \infty)$.
- Dependence between V and U is introduced via a bivariate copula using `VineCopula::BiCopSim`.

The simulator constructs two regressors internally (denoted x_1 and x_2).

Value

A list containing:

Y	Numeric vector of simulated dependent variable values.
X	Matrix of simulated independent variables (without intercept column).
V	Simulated two-sided noise term.
U	Simulated non-negative inefficiency term.
copula_uniforms	The simulated dependent uniforms from the copula (two columns).

Author(s)

Woraphon Yamaka, Paravee Maneejuk and Nuttaphong Kaewtathip

References

- Koenker, R. (2005). *Quantile Regression*. Cambridge University Press.
 Joe, H. (2014). *Dependence Modeling with Copulas*. Chapman & Hall/CRC.

Examples

```
sim_data <- sfa_simu_quantile(
  n = 100,
  beta = c(1, 0.5, -0.3),
  sigV = 1,
  sigU = 1,
  tau = 0.5,
  family = 1,
  rho = 0.3,
  seed = 123
)
str(sim_data)
```

 TE

Technical Efficiency Measure

Description

Computes technical efficiency for a copula-based stochastic frontier quantile model using simulation-based conditional expectations.

Usage

```
TE(theta, Y, X, family, tau,
  nSim = 200,
  rho2 = NULL,
  seed = NULL,
  plot = FALSE)
```

Arguments

theta	Numeric vector of estimated model parameters. The expected ordering is: regression coefficients (including intercept), σ_v , σ_u , copula parameter rho, and optionally rho2 if a two-parameter copula is used.
Y	Numeric vector of dependent variable observations.
X	Numeric matrix (or object coercible to a matrix) of independent variables (without intercept column).
family	Integer specifying the copula family (see <code>VineCopula::BiCopPDF</code>). Some families require a second parameter rho2.
tau	Quantile level in (0, 1) for the asymmetric Laplace distribution.
nSim	Number of Monte Carlo draws used to approximate the conditional expectation. Larger values reduce simulation noise but increase computation time.
rho2	Optional second copula parameter. If NULL and theta contains an additional element beyond rho, the function will use that element as rho2.
seed	Optional integer seed for reproducibility in simulation-based computation. If NULL, no seed is set.
plot	Logical. If TRUE, produces a plot of sorted technical efficiency values.

Details

Technical efficiency is computed as a simulated conditional expectation:

$$TE_i = E[\exp(-U_i) | w_i],$$

where $w_i = Y_i - x_i^\top \beta$ and the weights are constructed using the asymmetric Laplace density for the noise term and the copula density capturing dependence between the inefficiency component and the noise component.

The inefficiency term U is generated from a truncated asymmetric Laplace distribution on $(0, \infty)$.

If `plot = TRUE`, the function produces a line plot of sorted technical efficiency values.

Value

A numeric vector of technical efficiency values (one per observation).

Author(s)

Woraphon Yamaka, Paravee Maneejuk, and Nuttaphong Kaewtathip

References

Pipitpojanakarn, V., Maneejuk, P., Yamaka, W., & Sriboonchitta, S. (2016). Analysis of agricultural production in Asia and measurement of technical efficiency using copula-based stochastic frontier quantile model. In *International Symposium on Integrated Uncertainty in Knowledge Modelling and Decision Making* (pp. 701–714). Springer.

Examples

```
sim_data <- sfa_simu_quantile(  
  n = 100,  
  beta = c(1, 0.5, -0.3),  
  sigV = 1,  
  sigU = 1,  
  tau = 0.5,  
  family = 1,  
  rho = 0.3,  
  seed = 123  
)  
  
model <- copSQM(  
  Y = sim_data$Y,  
  X = sim_data$X,  
  family = 1,  
  tau = 0.5,  
  RHO = 0.3,  
  LB = -0.99,  
  UB = 0.99,  
  nSim = 50,  
  seed = 123  
)  
  
te_values <- TE(  
  theta = model$result[, "Estimate"],  
  Y = sim_data$Y,  
  X = sim_data$X,  
  family = 1,  
  tau = 0.5,  
  nSim = 200,  
  seed = 123,  
  plot = TRUE  
)  
  
head(te_values)
```

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